

Solve the equation:

$$2\cos^2\theta + \cos\theta - 1 = 0 \quad 0 \leq \theta < 2\pi$$

$$2\cos^2\theta + \cos\theta - 1 = 0$$

$$(2\cos\theta - 1)(\cos\theta + 1) = 0$$

$$2\cos\theta - 1 = 0 \quad \text{or} \quad \cos\theta + 1 = 0$$

$$\cos\theta = \frac{1}{2} \quad \text{or} \quad \cos\theta = -1$$

$$\theta = \frac{\pi}{3} \quad \theta = 2\pi - \frac{\pi}{3} = \frac{5\pi}{3} \quad \theta = \pi$$

Solve the equation:

$$\cos 2\theta + \sin^2\theta = \frac{3}{4} \quad 0 \leq \theta < 2\pi$$

$$\cos^2\theta - \sin^2\theta + \sin^2\theta = \frac{3}{4}$$

$$\cos^2\theta = \frac{3}{4} \quad \cos\theta = \pm \frac{\sqrt{3}}{2}$$

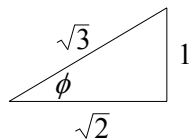
$$\theta = \frac{\pi}{6}, \pi - \frac{\pi}{6}, \pi + \frac{\pi}{6}, 2\pi - \frac{\pi}{6}$$

Solve: $\sqrt{2}\sin\theta + \cos\theta = 1, 0 \leq \theta < 2\pi$

$$r^2 = (\sqrt{2})^2 + 1^2 = 2 + 1 = 3 \quad r = \sqrt{3}$$

$$\frac{\sqrt{2}}{\sqrt{3}}\sin\theta + \frac{1}{\sqrt{3}}\cos\theta = \frac{1}{\sqrt{3}}$$

$$\cos\phi = \frac{\sqrt{2}}{\sqrt{3}} \quad \sin\phi = \frac{1}{\sqrt{3}}$$



$$\sin\theta\cos\phi + \sin\phi\cos\theta = \frac{1}{\sqrt{3}}$$

$$\sin(\theta + \phi) = \frac{1}{\sqrt{3}}$$

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$$\theta + \phi = \sin^{-1}\frac{1}{\sqrt{3}} \quad \theta + \phi = \pi - \sin^{-1}\frac{1}{\sqrt{3}}$$

$$\theta = \sin^{-1}\frac{1}{\sqrt{3}} - \phi \quad \theta = \pi - \sin^{-1}\frac{1}{\sqrt{3}} - \phi$$

$$\theta = \sin^{-1}\frac{1}{\sqrt{3}} - \sin^{-1}\frac{1}{\sqrt{3}} \quad \theta = \pi - \sin^{-1}\frac{1}{\sqrt{3}} - \sin^{-1}\frac{1}{\sqrt{3}}$$

$$\theta = 0$$

$$\theta = \pi - 2\sin^{-1}\frac{1}{\sqrt{3}}$$

Solve the equation $\sin\theta\cos\theta = -\frac{1}{2}$

$$2\sin\theta\cos\theta = -1$$

$$\sin 2\theta = -1$$

$$2\theta = \frac{3\pi}{2} + 2k\pi$$

$$\theta = \frac{3\pi}{4} + k\pi$$

$$\text{In } [0, 2\pi) \text{ use } \frac{3\pi}{4}, \frac{7\pi}{4}$$

Use a graphing utility to solve:

$$\cos x + x = 2$$