

Function name	Abbreviation	Value
sine of θ	$\sin \theta$	b / c
cosine of θ	$\cos \theta$	a / c
tangent of θ	$\tan \theta$	b / a
cosecant of θ	$\csc \theta$	c / b
secant of θ	$\sec \theta$	c / a
cotangent of θ	$\cot \theta$	a / b

“SOH CAH TOA”

Reciprocal Identities

$$\csc \theta = \frac{1}{\sin \theta} \quad \sec \theta = \frac{1}{\cos \theta} \quad \cot \theta = \frac{1}{\tan \theta}$$

Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$$

$$b^2 + a^2 = c^2$$

$$\frac{b^2}{c^2} + \frac{a^2}{c^2} = \frac{c^2}{c^2}$$

$$\left(\frac{b}{c}\right)^2 + \left(\frac{a}{c}\right)^2 = 1$$

$\sin^2 \theta + \cos^2 \theta = 1$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

θ (Degrees)

$$\sin \theta = \cos(90^\circ - \theta)$$

$$\cos \theta = \sin(90^\circ - \theta)$$

$$\tan \theta = \cot(90^\circ - \theta)$$

$$\cot \theta = \tan(90^\circ - \theta)$$

$$\sec \theta = \csc(90^\circ - \theta)$$

$$\csc \theta = \sec(90^\circ - \theta)$$

θ (Radians)

$$\sin \theta = \cos(\pi/2 - \theta)$$

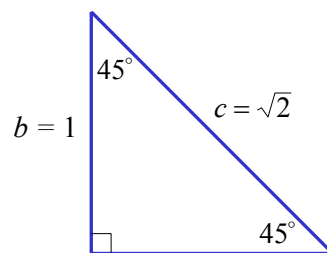
$$\cos \theta = \sin(\pi/2 - \theta)$$

$$\tan \theta = \cot(\pi/2 - \theta)$$

$$\cot \theta = \tan(\pi/2 - \theta)$$

$$\sec \theta = \csc(\pi/2 - \theta)$$

$$\csc \theta = \sec(\pi/2 - \theta)$$



$$a = 1$$

$$c^2 = a^2 + b^2 \quad c^2 = 1^2 + 1^2 = 2$$

$$c = \sqrt{2}$$

$$\sin 45^\circ = \sin \frac{\pi}{4} = \frac{b}{c} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

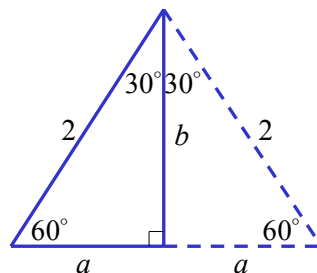
$$\cos 45^\circ = \cos \frac{\pi}{4} = \frac{a}{c} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

$$\tan 45^\circ = \tan \frac{\pi}{4} = \frac{b}{a} = \frac{1}{1} = 1$$

$$\cot 45^\circ = \cot \frac{\pi}{4} = \frac{a}{b} = \frac{1}{1} = 1$$

$$\csc 45^\circ = \csc \frac{\pi}{4} = \frac{c}{b} = \frac{\sqrt{2}}{1} = \sqrt{2}$$

$$\sec 45^\circ = \sec \frac{\pi}{4} = \frac{c}{a} = \frac{\sqrt{2}}{1} = \sqrt{2}$$



$$2a = 2 \text{ so } a = 1$$

$$2^2 = 1^2 + b^2$$

$$c^2 = a^2 + b^2$$

$$b^2 = 2^2 - 1^2 = 4 - 1 = 3$$

$$b = \sqrt{3}$$

$$\sin 60^\circ = \sin \frac{\pi}{3} = \frac{b}{c} = \frac{\sqrt{3}}{2} \quad \cos 60^\circ = \cos \frac{\pi}{3} = \frac{a}{c} = \frac{1}{2}$$

$$\tan 60^\circ = \tan \frac{\pi}{3} = \frac{\sin 60^\circ}{\cos 60^\circ} = \frac{\sqrt{3}/2}{1/2} = \frac{\sqrt{3}}{1} = \sqrt{3}$$

$$\cot 60^\circ = \cot \frac{\pi}{3} = \frac{1}{\tan 60^\circ} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

$$\csc 60^\circ = \csc \frac{\pi}{3} = \frac{1}{\sin 60^\circ} = \frac{1}{\sqrt{3}/2} = \frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

$$\sec 60^\circ = \sec \frac{\pi}{3} = \frac{1}{\cos 60^\circ} = \frac{1}{1/2} = 2$$

$$\sin 30^\circ = \sin \frac{\pi}{6} = \frac{a}{c} = \frac{1}{2} \quad \cos 30^\circ = \cos \frac{\pi}{6} = \frac{b}{c} = \frac{\sqrt{3}}{2}$$

$$\tan 30^\circ = \tan \frac{\pi}{6} = \frac{\sin 30^\circ}{\cos 30^\circ} = \frac{1/2}{\sqrt{3}/2} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

$$\cot 30^\circ = \cot \frac{\pi}{6} = \frac{1}{\tan 30^\circ} = \frac{1}{1/\sqrt{3}} = \sqrt{3}$$

$$\csc 30^\circ = \csc \frac{\pi}{6} = \frac{1}{\sin 30^\circ} = \frac{1}{1/2} = 2$$

$$\sec 30^\circ = \sec \frac{\pi}{6} = \frac{1}{\cos 30^\circ} = \frac{1}{\sqrt{3}/2} = \frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

Use a calculator to find the approximate value of

(a) $\sin 52^\circ$

(b) $\tan \frac{\pi}{5}$

(c) $\sec \frac{\pi}{5}$