

Name: \_\_\_\_\_

**Directions:** Show all work.

1. [**2 parts, 3 points each**] Graphs with specified degrees.
  - (a) Is there an 8-vertex graph in which half the vertices have degree 3 and the other half have degree 4? Either give an example or explain why not.

- (b) Is there a 10-vertex graph in which half the vertices have degree 3 and the other half have degree 4? Either give an example or explain why not.

2. [**4 points**] Use the Petersen graph (displayed below) to show that  $K_{10} \not\rightarrow K_3, K_5$ . What can we conclude about  $r(3, 5)$ ?

