**Directions:** Show all work.

1. [3 points] Suppose that  $A(x) = \frac{1}{(1-2x)^8}$ . What is the coefficient of  $x^{12}$  in A(x)?

2. [4 points] Suppose that  $(a_n)_{n\geq 0}$  has OGF  $A(x)=\frac{1}{(1-2x)(1-3x)}$ . Find a formula for  $a_n$ .

3. [3 points] Let  $a_0 = 2$ ,  $a_1 = 1$ , and  $a_n = 3a_{n-1} + a_{n-2} + 2^n$  for  $n \ge 2$ . Find the OGF A(x).