Directions: Solve the following problems. Give supporting work/justification where appropriate.

1. [2.5 points] Let x and y be real numbers. Prove that if x is rational and xy is irrational, then y is irrational.

2. [2.5 points] Let a and n be integers. Prove that if $a \mid n$ and $a \mid n+1$, then a=1 or a=-1.

3. [2.5 points] Let n be an odd positive integer. Prove that $\sqrt{2n}$ is irrational.

4. [2.5 points] Let n be an integer. Prove that $3 \nmid n^2 + 1$.