

Directions: You may work to solve these problems in groups, but all written work must be your own. **Show your work;** See “Guidelines and advice” on the course webpage for more information.

1. Compute the following sums.

(a) $3 + 6 + 9 + 12 + \cdots + 3n$

(b) $\sum_{k=1}^n (3k - 1)$.

(c) Let a and b be real numbers. Evaluate $\sum_{k=1}^n (ak + b)$. Show how your answer to part (c) generalizes your answers to parts (a) and (b).

2. [S 3.11.1] Decide whether each of the following statements is True or False. Briefly justify your answer. We define the following sets.

$$A = \{x \in \mathbb{Z} \mid -3 \leq x \leq 3\}$$

$$B = \{y \in \mathbb{Z} \mid -5 < y < 6\}$$

$$C = \{x \in \mathbb{R} \mid x^2 \geq 9\}$$

$$D = \{x \in \mathbb{R} \mid x < -3\}$$

$$E = \{n \in \mathbb{N} \mid n \text{ is even}\}$$

(a) $A \subseteq B$

(b) $C \cap D = \emptyset$

(c) $4 \in E \cap B$

(d) $\{4\} \subseteq A \cap E$

(e) $10 \in C - D$

(f) $A \cup B \supseteq C$

(g) $3 \in A \cap C$

(h) $0 \in (A - B) \cup D$

(i) $E \cap C \subseteq \mathbb{Z}$

(j) $0 \notin B - C$

3. Let $A = \{1, 2, 3, 4, 5, 6, 7, 8\}$ and let $B = \{\{1\}, \{2, 3, 4\}, \{5, 5, 6\}, 7\}$.

(a) Determine $|A|$ and $|B|$.

(b) Determine $A \cap B$.

(c) True or False: $\{4, 3, 2\} \in A$

(d) True or False: $\{4, 3, 2\} \in B$

(e) True or False: $\{5, 6\} \in A$

(f) True or False: $\{5, 6\} \in B$

(g) True or False: $\{5, 6\} \subseteq A$

(h) True or False: $\{5, 6\} \subseteq B$