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Directions: Show all work. No credit for answers without work.

1. [4 parts, 2 points each] Simplify the following expressions.

(a) $(a+b)^2$

$$= (a+b)(a+b)$$

$$= a^2 + ba + ab + b^2$$

$$= \boxed{a^2 + 2ab + b^2}$$

(b) $\frac{a}{b} + \frac{c}{d}$

$$= \frac{a}{b} \cdot \frac{d}{d} + \frac{c}{d} \cdot \frac{b}{b}$$

$$= \boxed{\frac{ad + cb}{bd}}$$

(c) $(\sqrt{x})^{-4} = \left(x^{\frac{1}{2}}\right)^{-4}$

$$= x^{-\frac{4}{2}}$$

$$= x^{-2}$$

$$= \boxed{\frac{1}{x^2}}$$

(d) $\frac{1}{1 + \frac{1}{x}}$

$$= \frac{1}{1 + \frac{1}{x}} = \frac{1}{\frac{x}{x} + \frac{1}{x}} = \frac{1}{\frac{x+1}{x}}$$

$$= \boxed{\frac{x}{x+1}}$$

2. [2 points] Solve the equation $(x+2)^2 = x+14$ for x . Find all solutions.

$$(x+2)^2 = x+14$$

$$x^2 + 4x + 4 = x + 14$$

$$x^2 + 3x - 10 = 0$$

$$(x+5)(x-2) = 0$$

$$x = -5 \text{ or } x = 2$$

Check:

$$x = -5: (-5+2)^2 = (-5)+14$$

$$9 = 9 \checkmark$$

$$x = 2: (2+2)^2 = 2+14$$

$$16 = 16 \checkmark$$

Solus:

$$\boxed{x = -5, x = 2}$$