

Name: \_\_\_\_\_

**Directions:** Show all work. No credit for answers without work.

1. [3 points] Find the general solution of the system with the following augmented matrix.

$$\left[ \begin{array}{ccccc} 2 & 4 & -1 & 1 & 13 \\ -1 & -2 & 3 & -1 & -14 \\ 3 & 6 & 1 & 0 & 7 \end{array} \right]$$

2. [2 points] Are the two matrices given below row equivalent? Explain why or why not.

$$A = \begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 3 \\ 2 & 6 \end{bmatrix}$$

3. [**3 points**] Find a quadratic polynomial  $f(t) = a + bt + ct^2$  such that  $f(-1) = 9$ ,  $f(1) = 5$ , and  $f'(-1) = -4$ .

4. [**2 parts, 1 point each**] Pivot columns and number of solutions.

(a) Suppose that every column in the *augmented* matrix of a linear system contains a pivot position. What can you conclude about the number of solutions to the system? Explain.

(b) Suppose that every column in the *coefficient* matrix of a linear system contains a pivot position. What can you conclude about the number of solutions to the system? Explain.