Directions: You may work to solve these problems in groups, but all written work must be your own. Show your work; See "Guidelines and advice" on the course webpage for more information.

1. Let $\Sigma=\{0,1\}$. Give state diagrams of DFAs for the following languages.
(a) $\{w \mid w$ begins with a 1 and ends with a 0$\}$.
(b) $\{w \mid w$ has an even number of 1 s or contains the substring 101$\}$
2. Let $N$ be the NFA pictured below.

(a) Which of the following strings are accepted by $N$ ? Explain. Strings: $\lambda, b, b b, b b b, b b b b$.
(b) Convert $N$ into an equivalent DFA.
3. Let $\Sigma=\{0,1\}$, let $A=\{w \mid w$ ends in a 1$\}$, and let $B=\{w \mid w$ has odd length $\}$. Construct a DFA with 4 states that recognizes the language $A B$. (Hint: it may be easier to first construct an NFA, convert to a DFA, and then simplify the DFA.)
