Directions: You may work to solve these problems in groups, but all written work must be your own. **Show your work**; See "Guidelines and advice" on the course webpage for more information.

- 1. Let $\Sigma = \{0, 1\}$. Give state diagrams of DFAs for the following languages.
 - (a) $\{w \mid w \text{ begins with a 1 and ends with a 0}\}.$
 - (b) $\{w \mid w \text{ has an even number of 1s or contains the substring 101}\}$
- 2. Let N be the NFA pictured below.



- (a) Which of the following strings are accepted by N? Explain. Strings: λ , b, bb, bbb, bbbb.
- (b) Convert N into an equivalent DFA.
- 3. Let $\Sigma = \{0, 1\}$, let $A = \{w \mid w \text{ ends in a } 1\}$, and let $B = \{w \mid w \text{ has odd length}\}$. Construct a DFA with 4 states that recognizes the language AB. (Hint: it may be easier to first construct an NFA, convert to a DFA, and then simplify the DFA.)