

Name: _____

1. [**2 parts, 2 points each**] Convert the following functions to the form $R \cos(\omega_0 t - \delta)$.

(a) $4 \cos(2t) - 3 \sin(2t)$

(b) $-7 \cos(t) + 2 \sin(t)$

2. [**1 point**] An object of mass m (kg) is attached to a spring with spring constant k (kg/s²). The system is damped with damping constant γ (kg/s). The system is critically damped if and only if m , γ , and k satisfy a certain equation. What is this equation? (Hint: if you do not have this memorized, derive it directly from the differential equation that models spring/mass systems.)

3. A mass of 250 grams stretches a spring 8 cm. The system is undamped. Initially, the mass is pushed up a distance of 2 cm from its equilibrium position and released with a downward velocity of 10 cm/s.

(a) [**3 points**] Find the position $u(t)$ of the spring at time t . Express u in cm and t in s.

(b) [**2 points**] Determine the maximum distance of the mass from its equilibrium position and the time when it first reaches this position. Hint: first express $u(t)$ in the form $u(t) = R \cos(\omega_0 t - \delta)$.