

Name: Solution Key

1. [3 points] Simplify $\frac{2x+b-3}{x-4} - \frac{x+5}{3x}$.

$$\frac{(2x+b-3)3x}{(x-4)3x} - \frac{(x+5)(x-4)}{3x(x-4)}$$

$$= \frac{6x^2 + 3bx - 9x}{3x^2 - 12x} - \frac{x^2 + x - 20}{3x^2 - 12x}$$

$$= \frac{6x^2 + 3bx - 9x - x^2 - x + 20}{3x^2 - 12x}$$

$$= \boxed{\frac{5x^2 + 3bx - 10x + 20}{3x^2 - 12x}}$$

2. [2 points] Simplify $\frac{5x^{3/2}}{x} + \sqrt{x}$.

$$5x^{1/2} + x^{1/2}$$

$$= \boxed{6x^{1/2}}$$

$$= \boxed{6\sqrt{x}}$$

3. [2 points] Find all solutions to the equation $x^2 + 6x - 40 = 0$.

$$(x - 4)(x + 10) = 0$$

$$\boxed{x = +4 \text{ or } x = -10}$$

4. [3 points] Find all solutions to the equation $6 = t + \sqrt{76 - 15t}$.

$$6 - t = \sqrt{76 - 15t}$$

$$(6 - t)^2 = 76 - 15t$$

$$36 - 12t + t^2 = 76 - 15t$$

$$t^2 + 3t - 40 = 0$$

$$(t + 8)(t - 5) = 0$$

$$t = -8 \text{ or } t = 5.$$

Check: $t = -8: 6 - (-8) = \sqrt{76 - 15(-8)}$
 $14 = \sqrt{76 + 120}$
 $14 = \sqrt{196} \checkmark$

$t = 5: 6 - 5 = \sqrt{76 - 15 \cdot 5}$
 $1 = \sqrt{1} \checkmark$

$\boxed{\text{Both } t = -8 \text{ and } t = 5 \text{ are solutions}}$

5. Have you taken a calculus class before?

Yes

6. If you could have dinner with any person dead or alive, who would it be, and why?

Paul Erdős, to work on reducing my

"Erdős" number