EXAM-I FALL 2006

MATH 261: Elementary Differential Equations EXAMINATION COVER PAGE

MATH 261 Professor Moseley

22

Total

101

PRINT	Last Name,	First Name	MI	(What you	wish to be	<u>)</u>
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ID #			_ EXAM DATE _	Friday, Sep	<u>tember 15,</u> Scores	
I swear	and/or affirm that all of the	he work presented on t	his exam is my own	page	points	score
and that	I have neither given nor	received any help durin	ng the exam.	1	10	
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	sides this cover page, the this exam. MAKE SUR	101	-	4	6	
pag	ge is missing, you will rec	eive a grade of zero fo	r that page. Read	5	7	
	ough the entire exam. If I will come to you.	you cannot read anythi	ng, raise your hand	6	8	
2. Pla	ce your I.D. on your desl	0		7	5	
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3. Pag	you wish. Print your name on all sheets.3. Pages 1-13 are multiple choice. Expect no part credit on these pages.				9	
	ere are no free response pould explain your solution	-	-	11	5	
ma	y be graded, not just you	r final answer. SHOW	YOUR WORK!	12	2	
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Proof-read your solutions and challows. GOOD LUCK!!!!!!!		• •	· ·	14		
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	DEQUES			16		
DL		T FOR REGRADE	These (ad) (1	17		
Please regrade the following problems for the reasons I ha (e.g., I do not understand what I did wrong on page			18			
				19		
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(Regra	ides should be requested	within a week of the da	te the exam is	21		

(Regrades should be requested within a week of the date the exam is returned. Attach additional sheets as necessary to explain your reasons.) I swear and/or affirm that upon the return of this exam I have **written nothing on this exam** except on this REGRADE FORM. (Writing or changing **anything** is considered to be cheating.)

Date _

Signature_

MATH 261	EXAM I	Fall 2006	Prof. Moseley	Page 1		
PRINT NAME						
1. (1 pt.) The orde	or of the ODE $y''' + 2$	$2x^{5}(y')^{2} = \cos x$ is _	A	ABCDE		
2. (1 pt.) The orde	er of the ODE $y^V +$	$e^{3x} y'' = \tan x$ is	·	ABCDE		
	ers for questions 1 and C) 3 D) 4 E) 5		AD) 8 AE) None o	f the previous		
True or False	Circle True or False	, but not both. If I car	nnot read your answer, it	is wrong.		
3.(1 pt.) A) True	or B)False The ODE	$z y''' + 2x^5 y'' = \cos x$	x is linear (y as a functi	on of x).		
4. (1 pt.) A) True	or B)False The ODE	$E y^{VI} + e^{3x} y'' y = tar$	n x is linear (y as a funct	ion of x).		
5. (1 pt.) A)True o		an infinite number of $+ x y = 0$.	functions that satisfy the			
6. (1 pt.) A)True o			= g(x) where p(x) and g(x ntegrating factor given by			
7. (1 pt.) A)True o			x) $y = g(x)$, where $p(x)$ as ways obtain y explicitly as	-		
8. (1 pt.) A)True o	the IVP:	-	taining qualitative inform y_0 , even if the solution can			
9. (1 pt.) A)True o		-	ntegrating factors that wi are not exact to ones that			
10. (1 pt.) A)True		ifferential equations ar	n Bernoulli helped to dev nd to extend the range of	_		

Possible points this page = 10. POINTS EARNED THIS PAGE = _____

Prof. Moseley

PRINT NAME () ID No.

Last Name, First Name MI What you wish to be called

True or False. For the given first order ODEs, determine if the statements below are true or false. The statements relate to possible methods of solution. Recall from class that the possible methods are:

- 1) First order linear (y as a function of x).- Integrating factor = $\mu = \exp(\int p(x) dx$)
- 2) First order linear (x as a function of y).- Integrating factor = $\mu = exp(\int p(y) dy)$)
- 3) Separable.
- 4) Exact Equation (Must be exact in one of the two forms discussed in class).
- 5) Bernoulli, but not linear (y as a function of x). Use the substitution $v = y^{1-n}$.
- 6) Bernoulli, but not linear (x as a function of y). Use the substitution $v = x^{1-n}$.
- 7) Homogeneous, but not separable. Use the substitution v = y/x or v = x/y.
- 8) None of the above techniques works.

Also recall the following:

- a. In this context, exact means exact as given in either of the forms discussed in class. (Attendance is mandatory.)
- b. Bernoulli is not a correct method of solution if the original equation is linear.
- c. Homogeneous is not a correct method of solution if the original equation is separable.

Circle True or False, but not both. If I cannot read your answer, it is wrong. DO NOT SOLVE.

 $(*)(y^3 + x^2y) dx + x^3 dy = 0$

11.(2 pts.) A)True or B)False (*) is a linear ode (y as a function of x).

12. (2 pts.) A)True or B)False (*) is a Bernoulli ode (y as a function of x).

13. (2 pts.) A)True or B)False (*) is a homogeneous ode

(#) ($x^2 + 2xy$) dx + x^2 dy = 0

- 14. (2 pts.) A)True or B)False (#) is a linear ode (y as a function of x).
- 15. (2 pts.) A)True or B)False (#) is an exact ode.
- 16. (2 pts.) A)True or B)False (#) is a separable ode

) ID No.

PRINT NAME _____

Last Name, First Name MI What you wish to be called

True or False. For the given first order ODEs, determine if the statements below are true or false. The statements relate to possible methods of solution. Recall from class that the possible methods are:

1) First order linear (y as a function of x).- Integrating factor = $\mu = \exp(\int p(x) dx$)

2) First order linear (x as a function of y).- Integrating factor = $\mu = \exp(\int p(y) dy$)

3) Separable.

4) Exact Equation (Must be exact in one of the two forms discussed in class).

5) Bernoulli, but not linear (y as a function of x). Use the substitution $v = y^{1-n}$.

6) Bernoulli, but not linear (x as a function of y). Use the substitution $v = x^{1-n}$.

7) Homogeneous, but not separable. Use the substitution v = y/x or v = x/y.

8) None of the above techniques works.

Also recall the following:

a. In this context, exact means exact as given in either of the forms discussed in class. (Attendance is mandatory.)

b. Bernoulli is not a correct method of solution if the original equation is linear.

c. Homogeneous is not a correct method of solution if the original equation is separable.

Circle True or False, but not both. If I cannot read your answer, it is wrong.

(*)
$$(3x^2y + 2xy) dx + (x^3 + x^2) dy = 0$$

17. (2 pts.) A)True or B)False . (*) is a linear ode (y as a function of x).

18. (2 pts.) A)True or B)False (*) is a separable ode.

19. (2 pts.) A)True or B)False (*) is an exact ode.

(#) (4x + y) dx + (x + 3y) dy = 0

20. (2 pts.) A)True or B)False (#) is a linear ode (y as a function of x).

21. (2 pts.) A)True or B)False (#) is an exact ode.

22. (2 pts.) A)True or B)False (#) is a separable ode

Total points this page = 12. TOTAL POINTS EARNED THIS PAGE _____

PRINT NAME(______) ID No.Last Name, First Name MI What you wish to be calledFor each question write your answer in the blank provided. Next find your answer from the listof possible answers listed below and write the corresponding letter or letters for your answer inthe blank provided. Then circle this letter or letters. Finally, circle your answer. Consider theOrdinary Differential Equation (ODE):y' = 2y + sin(x),

23. (1 pts.) To solve this ODE we first put it in the standard form for solving first order linear

ODE's given by ______. A B C D E . (Be careful. No part credit for this problem. Hence if you miss this part, it may cause you to miss all parts): A) $y' = 2y + \sin(x)$ (It's already in the appropriate form for solving a first order linear ODE) B) $y' + 2y + \sin(x) = 0$ C) $y' - 2y = \sin(x)$ D) $y' + 2y = \sin(x)$ E) $y' - 2y - \sin(x) = 0$ AB) None of the above

24. (2 pts.) An integrating factor μ for this linear ODE given above is given by

 $\begin{array}{cccc} & & & \\ A) & \mu = 2x & B) & \mu = \sin(x) \\ AB) & \mu = & e^{-2x} & AC) & \mu = & e^x \end{array} \begin{array}{c} A & B & C & D & E \\ C) & \mu = & e^{\sin(x)} & D) & \mu = & e^{2x} & E) & \mu = & e^{-\sin(x)} \\ AD) & \mu = & e^{-x} & AE) & \text{None of the above} \end{array}$

25. (3 pts.) In solving the linear Ordinary Differential Equation (ODE) given above, the

following steps occurs ______. A B C D E
A)
$$\frac{d(ye^{-2x})}{dx} = e^{-2x} \sin(x)$$
 B) $\frac{d(ye^{\cos(x)})}{dx} = x^2 e^{\cos(x)}$ C) $\frac{d(ye^{2x})}{dx} = e^{2x} \sin(x)$
D) $\frac{d(ye^{2x})}{dx} = e^{2x} \cos(x)$ E) $\frac{d(ye^{-2x})}{dx} = e^{-2x} \cos(x)$ AB) $\frac{d(ye^{-2x})}{dx} = xe^{-2x}$
AC) $\frac{d(ye^{2x})}{dx} = x \cos(x)$ AD) None of the above steps ever appears in any solution of this problem.

A) $y = x + 1 + ce^{x}$ B) $y = -x + 1 + ce^{x}$ C) $y = x - 1 + ce^{x}$ D) $y = x + 1 + ce^{-x}$ E) $y = -x + 1 + ce^{-x}$ AB) $y = x - 1 + ce^{-x}$ AC) $y = -x - 1 + ce^{-x}$ AD) $y = x + 1 + e^{x} + c$ AE) $y = -x + 1 + e^{x} + c$ BC) $y = x - 1 + e^{x} + c$ BD) $y = x + 1 + e^{-x} + c$ BE) $y = -x + 1 + e^{-x} + c$ CD) $y = x - 1 + e^{-x} + c$ CE). $y = x + 1 - e^{-x} + c$ DE) None of the above families of solutions is correct.

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L	ast Name, First Nan	he MI, What	you wish to	be called		
For each question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters.						
28. (3 pts.) Suppose that the general solution of the ODE $y' = f(x,y)$ is $y = x + ce^{2x}$.						
Solve the IVP. ODE $y' = f(x,y)$ IC $y(0) = 2$						
The value of the function you found as the solution to the IVP at $x = 1$ is						
$y_{ x=1} = =$ A B C D E						

29. (5 pts.) Solve the IVP ODE dy/dx = x/y IC $y(0) = \sqrt{3}$ The value of the function you found as the solution to the IVP at x = 1 is

y,	_ =		ABCDE
	$\mathbf{x} = 1$		

Possible answers this page. A) 0 B) 1 C) 2 D) 3 E) 4 AB) $1 + 2e^2$ AC) $1 + 2e^{-1}$ AD) $1 + 2e^{-2}$ AE) $1 + 2\pi^{-1}$ BC) $\frac{1}{2}$ BD) $\frac{1}{3}$ BE) π CD) $1 + \sqrt{3}$ CE) $1 + 2\sqrt{3}$ DE) $2 + 2\sqrt{3}$ ABC) None of the above. Possible points this page = 8. POINTS EARNED THIS PAGE = _____ PRINT NAME () ID No.

Last Name. First Name MI What you wish to be called

For this question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer in the list below. Consider

 $(2x + y^2) dx + (2xy) dy = 0.$ ODE

30. (5 pts.) The solution to the ODE is ______. A B C D E Be careful with your computations as there will be no part credit for an incorrect answer.

A) $\psi(x,y) = x^2 + xy^2$ D) $\psi(x,y) = x^2 + 2xy^2 + C$ E) $x^2 + xy^2 = C$ AB) $x^2 + 2xy^2 = C$ AC). $x^2 + 2y^2 = C$ AD) $x^2 + y^2 = C$ AE) None of the above. Possible points this page = 5. TOTAL POINTS EARNED _____

PRINT NAME _______ (______) ID No. ______

Last Name. First Name MI What you wish to be called For each question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer. Consider the ODE $dy/dx = e^{y/x}$.

- 31. (1 pt). The appropriate classification for the ODE is ______. A B C D E
 A) Exact Equation B) Bernoulli (y as a function of x) C) Bernoulli (x as a function of y).
 D) Homogeneous E) None of the above techniques works.
- 32. (2 pts.) An appropriate substitution (change of variable) to convert the given ODE

is ______. A B C D E
A)
$$v = 1/y$$
 B) $v = 1/y^2$ C) $v = y^2$ D) $v = 1/y^3$ E) $v = y/x$ AB) $v = y^3$ AC) $v = \sqrt{y}$
D) None of the above

AD) None of the above.

33. (2 pts.)The correct term for dy/dx in terms of x and v for this substitution

is ______. A B C D E
A)
$$\frac{dy}{dx} = \frac{1}{2}v^{-\frac{1}{2}}\frac{dv}{dx}$$
 B) $\frac{dy}{dx} = -\frac{1}{2}v^{-\frac{1}{2}}\frac{dv}{dx}$ C) $\frac{dy}{dx} = \frac{1}{2}v^{-\frac{3}{2}}\frac{dv}{dx}$ D) $\frac{dy}{dx} = -\frac{1}{2}v^{-\frac{3}{2}}$
E) $\frac{dy}{dx} = v + x\frac{dv}{dx}$ AB) $\frac{dy}{dx} = -v + x\frac{dy}{dx}$ AC)None of the above.

34. (3 pts.) The new ODE that is derived is ______. A B C D E A) $x \frac{dv}{dx} = e^v - 2v$ B) $x \frac{dv}{dx} = e^v - v$ C) $x \frac{dv}{dx} = e^{-v} - v$ D) $x \frac{dv}{dx} = e^v - 4v$ E) $x \frac{dv}{dx} = -e^v - v$ AB) $\frac{dv}{dx} = -e^v + v$ AC) None of the above.

35. (2 pts.) The correct classification of the new ODE that you derived

is _____. A B C D E

(Do not solve this equation.)

A) First order linear (v as a function of x), B) First order linear (x as a function of v)

C) Separable. D) Exact E) None of the above.

PRINT NAME () ID No.

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For each question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer in the list. Consider the ODE $dy/dx = 2xy + 4y^3$.

- 36. (1 pt) The appropriate classification for this ODE is ______. A B C D EA) Exact B) Bernoulli (y as a function of x) C) Bernoulli (x as a function of y).

 - D) Homogeneous E) None of the above techniques works.
- 37. (2 pts.) An appropriate substitution (change of variable) to convert the given ODE is ______. A B C D E ______. A B C D E ______. A B C V = $1/y^2$ ______. D v = y/x _______. B) v = $1/y^3$ ______. AB) v = y^3 _______. AC) v = \sqrt{y} _______. AD) A) v

None of the above.

38. (2 pts.)The correct term for dy/dx in terms of x and v for this substitution

___. ____A B C D E A) $\frac{dy}{dx} = -\frac{1}{2}v^{-\frac{1}{2}}\frac{dv}{dx}$ B) $\frac{dy}{dx} = \frac{1}{2}v^{-\frac{1}{2}}\frac{dv}{dx}$ C) $\frac{dy}{dx} = \frac{1}{2}v^{-\frac{3}{2}}\frac{dv}{dx}$ D) $\frac{dy}{dx} = -\frac{1}{2}v^{-\frac{3}{2}}\frac{dv}{dx}$ E) $\frac{dy}{dx} = -\frac{3}{2}v^{\frac{3}{2}}\frac{dv}{dx}$ AB) $\frac{dy}{dx} = -\frac{3}{2}v^{-\frac{3}{2}}\frac{dy}{dx}$ AC)None of the above.

39. (3 pts.) The new ODE that is derived is _____ _____. ____A B C D E A) $\frac{dv}{dx} + 4x v = 8$ B) $\frac{dv}{dx} + 2x v = 4$ C) $\frac{dv}{dx} + 4x v = 8$ D) $\frac{dv}{dx} - 4x v = 8$ E) $\frac{dv}{dx} - 4x v = -8$ AB) $\frac{dv}{dx} + 4x v = -8$ AC) None of the above.

40. (2 pts.) The correct classification of the new ODE that you derived

- Is ______. A B C D E A) First order linear (v as a function of x), B) First order linear (x as a function of v)
- C) Separable. D) Exact Equation E) None of the above.

ABCDE

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Last Name. First Name MI What you wish to be called

For each question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer in the list. Suppose that the ODE dy/dx = f(x,y) is not linear or separable, but that it can be solved using the substitution (change of variable), v = y/x. Suppose further that this substitution results in

the derived ODE
$$v + x \frac{dv}{dx} = v^2$$
.

41. (2 pts.) The correct classification of the new derived ODE

C) Separable D) Exact E) None of the above.

42. (5 pts.) The solution of the derived ODE is ______.

A)
$$v = \frac{x}{1-cx}$$
 B) $v = \frac{1}{1-cx}$ C) $v = \frac{x^2}{1-cx}$ D) $v = \frac{x}{1-x}$ E) $v = \frac{x}{2-cx}$ AB) $v = \frac{x}{x-c}$

AC)None of the above.

43. (2 pts.) The solution of the original ODE is ______. A B C D E A) $y = \frac{x}{1-cx}$ B) $y = \frac{1}{1-cx}$ C) $y = \frac{x^2}{1-cx}$ D) $y = \frac{x}{1-x}$ E) $y = \frac{x}{2-cx}$ AB) $y = \frac{x}{x-c}$ AC) None of the above.

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44. (1 pt) The fu	ndamental physical lav	w needed to develop th	ne model			
is			A B C D E			
A) Ohm's law B) Conservation of mass C) Conservation of energy D) Kirchoff's lawE) Newton's second law (Conservation of momentum) AB) None of the above.						
45. (2 pts.)The mathematical model for the particle in a fluid system whose solution yields the downward velocity v(t) of the particle as a function of time						
is			A B C D E			
A) $\dot{mv} = mg + kv^3$ B) $\dot{mv} = mg - kv^3$ C) $\dot{mv} = -mg - kv^3$ D) $\dot{mv} = -mg - kv^3$ $v(0) = v_0 \ge 0$ E) $\dot{mv} = mg - kv^3$ $v(0) = v_0 \ge 0$ AB) $\dot{mv} = -mg - kv^3$ $v(0) = v_0 \ge 0$ AC) None of the above. 46. (1 pt.) The units for the ODE in the model you selected in question ove						
are			A B C D E			
A) Feet H AB) Slugs		eet per second D) fe D) None of the above	et per second squared E) Pounds			
47. (1 pt.) A)Tru	ue or B)False If the p	particle is dropped, the	model given in question 45 above ca	n		

47. (1 pt.) A)True or B)False If the particle is dropped, the model given in question 45 above be solved to obtain a general formula for v without additional data.

Last Name, First Name MI What you wish to be called

For this question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer in the list.

MATHEMATICAL MODELING. Consider the following applied math problem:

An object (point particle) of mass 10 slugs is dropped from rest at time t = 0 in a medium that offers resistance equal to three times the cube of the velocity of the object where the velocity is measured in feet per second.

Apply the data given above to the general model you developed on the previous page to obtain the **specific model** for this problem. **DO NOT SOLVE!**

48. (2 pts.)The mathematical model for the system whose solution yields the velocity v(t) as a function of time

is				A B C D E
A)	10iv=320+3v ³ v(0)=0	B) $10\dot{v} = 320 - 3v^3$	C) $10\dot{v} = 320 - 10kv^3$	$D)10\dot{v} = 320 - 3v^3 v(0) = 0$

E) $10\dot{v} = -320 + 3v^3$ v(0) = 0 AB) $10\dot{v} = -320 - 3v^3$ v(0) = 3 AC) None of the above

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PRINT NAME _______ (_____) ID No. ______ Last Name, First Name MI What you wish to be called

For each question write your answer in the blank provided. Next find your answer from the list of possible answers listed below and write the corresponding letter or letters for your answer in the blank provided. Then circle this letter or letters. Finally, circle your answer in the list.

49. (5 pts.) The direction field for the ODE y' = (3-y)/2 is given below. On this direction field are five curves labeled 1, 2, 3, 4, and 5 that were correctly or incorrectly drawn using the direction field. Consider the initial value problem (IVP):

IVP $\frac{ODE}{IC}$ y' = (3-y)/2y(0) = 4

The curve or curves that is the solution to this IVP is ______. ____A B C D E (Hint: Do not solve the IVP.)

 A) 1
 B) 2
 C) 3
 D) 4
 E) 5
 F) 1 and 2
 AB) 2 and 3
 AC). 3 and 4

 AD) 4 and 5
 AE) 1, 2, and 3
 BC) 2, 3, and 4
 BD) 3, 4, and 5

 BE) 1, 2, 3, 4, and 5
 CD) None of the above

Total points this page = 5. TOTAL POINTS EARNED THIS PAGE _____