MATH 251: STUDY GUIDE AND ASSIGNMENT SHEET

Textbooks: "Essential Calculus – Early Transcendentals" by Stewart, published by Thomson Brooks/Cole, 2007 Abbreviation. EC. "Linear Algebra for Calculus" (a supplement to the above text) by Heuvers, etc. Abbreviation LAC. "Linear Algebra Notes" Chapter 3 and 5 by James L. Moseley Abbreviation. LAN. Assignments are from these texts except that (A) indicates additional problems which are to be solved in the same assignment. These should be considered as minimal. Students who have difficulty as well as students who wish to acquire better than an average proficiency should work additional problems. The objective of this course is to provide an introduction to Linear Algebra, a reasonably complete coverage of fundamentals of multivariate calculus and an introduction to Vector Calculus. Additional coverage is contained in other courses. A change from the previous syllabus is that a better job of teaching the Linear Theory is attempted. Thus we now cover Vector Space Theory in slightly more detail. This will help students who also take Math 261 to understand how Linear Theory is used to solve Linear Differential Equations. Although a deep understanding of Vector Space Theory is not expected, coverage of the Algebraic Definition of the Dimension of a Subspace is expected. There are 39 assignments. At least 30 should be covered. Those with an asterisk(*) can be omitted without seriously impairing the objective of the course. Four hour (50 min.) exams and a comprehensive final should be given.

| Text, Ch, § | Material to be studied. | Problems to be worked in what text |
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| | INTRO. TO LIN. ALG. | LAC, LAN, and EC as specified |
| 1. LAN Ch. 2 | Matrix Oper. and Prop. | LAN Ch.2 p.11 #1-4, p.15 #1-5, p. 24 #1-4, p.28 #1, p.32#1-10 |
| 2. LAN Ch.3 | Vector Space and Subspace | LAN Ch.3 p.4#1-8, p.8 #1-4, p.12 #1-5 (A)Is W ={(x,y,0):x,y $\in \mathbf{R}$ }a subspace of \mathbf{R}^3 |
| 3.LAC Ch.2 | How to Solve $A\vec{x} = \vec{b}$ | LAC p.22 1abc, 2abc, 3, 5, 6 |
| 4. LAC Ch.3 | How to Solve $A\vec{x} = \vec{b}$ | LAC p.42 1def, 2befh, 3abcde, 4abcd, 5, 7 |
| 5. LAN Ch.5 | Operators, Spans | LAN Chap.5 p.3 #1-5, p.6 #1-12 |
| 6. LAN Ch.5 | Lin. Ind., Basis, Dim. | LAN Chap.5 p.11 #`1-11,p.14 #1-8, (A)Are the following sets linearly independent? $1.\{e^{3x},e^{3(x-1)}\}$ 2. $\{3t-5, 9t-15\}$ 3. $\{x^3, x ^3\}$ |
| 7. LAC Ch. 4 | Deter., Cramer's Rule | LAC p. 59 1-4, 9ab, 10 |
| 8. LAC Ch. 5 | Inverse of a Matrix | LAC p. 73 1-5, 6cde, 9, 15bc, 16ab |
| | <u>VECTORS AND THE,</u> <u>GEOM. OF SPACE</u> | Chapter 10 of "Essential Calculus – Early Transcendentals" by Stewart. p.517 |
| 9.EC§10.1 | 3-D Coordinate Systems | EC p521 #1-27 odd |
| 10.EC§10.2 | Vectors | EC.p.529 #1-21 odd,27,29 |
| 11.EC§10.3 | Dot Product | EC p.535 #1-25 odd, 31. |
| 12.EC§10.4 | Cross Product | EC p.543 #1-17 odd, 23-35 odd |
| 13. EC§10.5 | Eqs. of Lines and Planes | EC p.551 #1-43 odd |
| 14 EC§10.6 | Cylinders | EC p. 558 #1-8 odd |
| 15. EC§10.7 | Vec. Func.&Space Cur. | EC p.568 #1-27 odd, 33-51 odd, 57-65 odd |
| 16.EC §10.8 | Arc Length.& Curvature | EC p.576 #1,3, 7-27 odd,35, 37,41 |
| 17 EC §10.9 | Motion in Space | EC p.586 #1-11 odd, 15-21 odd, 29-33 odd. |
| 18.EC §10.6 | Quadric Surfaces | EC p.558 #9-15 odd . (Sketching) |

| 19.EC §10.6 | Quadric Surfaces | EC p.558 # 17-23 odd (Sketching) |
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| | <u>PARTIAL</u> <u>DERIVATIVES</u> | Chapter 11 of "Essential Calculus – Early Transcendentals" by Stewart. p.591 |
| 20. EC §11.1 | Func. of Several Var. | EC p.599#1-35 odd, 41-47 odd, 51 |
| 21. EC§11.2 | Limits and Continuity | EC p.608 #1-15 odd, 19-27 odd, 29,30 |
| 22 EC §11.3 | Partial Derivatives | EC p.614 #1-33 odd, 37-53 odd, 65,71. |
| 22 EC §11.4 | Tang.Pl.&Linear Appr. | EC p.624 #1-5, odd, 11-27 odd, 31 |
| 23 EC §11.5 | Chain Rule | EC p.631 #1-25 odd, 29,33,39 |
| 24.EC §11.6 | Dir. Der.&Grad Vec. | EC p.642 #1- 25 odd, 31,33,37 |
| 25. EC §11.7 | Max & Min | EC p.650 #1-13 odd, 23-27 odd, 31-45 odd |
| 26. EC§12.6, §12.6 | Cylind.&Spher. Coord. Coordinate Surfaces. | EC p.706 #1-13 p.711 # 1-14 |
| | <u>MULTIPLE</u> INTEGRALS | Chapter 12 of "Essential Calculus – Early Transcendentals" by Stewart. p.663 |
| 27.EC §12.1 | Double Integ. over Rec. | EC p.672 #1-33 odd, 37,39 |
| 29. EC§12.2 | Double Int .Over Regs. | EC p.680 #1-27 odd, 31-41 odd, 48, 51. |
| 30.EC §12.3 | Double Int. In Polar Cor | EC p.686 #1-17 odd, 23-29 odd |
| 31.EC §12.4 | Applications | EC p.693 #1-13 odd |
| 32.EC §12.5 | Triple Integrals | EC p.700 #1-19 odd, 25,31,37 |
| 33.EC §12.6 | Trip. Int. in Cyl. Coor. | EC p.706 #1-13 odd, 17,21 |
| 34.EC §12.7 | Trip Int. in Sph. Coor. | EC p.711 #1-15 odd, 21,23 |
| *35.EC §12.8 | Change of Variables | EC p.721 #1-15 odd, 19-23 odd |
| | VECTOR CALCULUS | Chapter 13 of "Essential Calculus – Early Transcendentals" by Stewart. p.725 |
| 36.EC §13.1 | Vector Fields | EC p.730 #1-17 odd, 21-25 odd, 29,31 |
| 37.EC §13.2 | Line Integrals | EC p.740 #1-19 odd, 27,33,35 |
| 38.EC §13.3 | Fund. Thm. Line Int. | EC p.749 #1-21 odd |
| 37.EC §13.4 | Green's Theorem | EC p.756 #1,3,7-19 odd |
| 38.EC §13.5 | Curl & Divergence | EC p.763#1-7 odd |
| *39.EC§13.6 | Para. Surfaces. | Ecp. 773#1,3 |
| *40.EC§13.7 | Surface Integrals | No problems |
| *41.EC§13.8 | Stokes' Theorem | No Problems |
| *42.EC§13.9 | Divergence Theorem | No Problems |